The interaction operator from PEC to ES can be derived from Eq. (20) by setting $M_1 = 0$. Moreover, the interaction operator from ES to PEC is

$$
\begin{align*}
\begin{bmatrix}
J_2 \\
\frac{1}{\eta} L_1 \\
\frac{1}{\eta} L_2
\end{bmatrix} = L_{ij} \begin{bmatrix}
J_i \\
\frac{1}{\eta} M_i \\
\frac{1}{\eta} L_i
\end{bmatrix} = \begin{bmatrix}
J_{i1} \\
\frac{1}{\eta} M_{i1} \\
\frac{1}{\eta} L_{i1}
\end{bmatrix}
\end{align*}
$$

(22)

Hence, the equation for the example in Figure 2 can be written as the following,

$$
\begin{align*}
\begin{bmatrix}
L_{11} & L_{12} \\
L_{21} & L_{22}
\end{bmatrix} \begin{bmatrix}
J_1 \\
\frac{1}{\eta} M_1 \\
\frac{1}{\eta} L_1
\end{bmatrix} + \begin{bmatrix}
J_{eq} \\
\frac{1}{\eta} M_{eq} \\
\frac{1}{\eta} L_{eq}
\end{bmatrix} &= - \begin{bmatrix}
L_{10} \\
L_{20}
\end{bmatrix} \begin{bmatrix}
J_0 \\
\frac{1}{\eta} M_0 \\
\frac{1}{\eta} L_0
\end{bmatrix} \\
- S_{22} \cdot T_{21}
\end{align*}
$$

(23)

4. NUMERICAL EXAMPLES

Here we will show one example of a two-monopole array mounted on a ground plane as shown in Figure 3(a). Two ES’s that intercept the ground plane are used to enclose the antennas [Fig. 3(b)]. Triangular mesh and RWG basis [11] are used to discretize the structure. There are 779 unknowns on the whole antenna and 476 unknowns on each ES. The simulation frequency is 0.3 GHz, and the length of the monopole is a quarter wavelength. The excitation is a multiple-

$$
\begin{align*}
\text{gap source added on the left arm. Figure 4 shows the equivalent current distribution, and Figure 5(b) shows the radiation field using the direct method and EPA. The two results agree with each other very well.}
\end{align*}
$$

5. CONCLUSIONS

The equivalence principle algorithm is introduced in this communication. It is based on MOM and equivalence principle. Tap basis is introduced to model a continuous current intercepting the equivalent surface. Using this scheme, the current continuity is conserved and the singularity of the charges is avoided. Moreover, it is more stable and accurate than using a fictitious junction basis.

REFERENCES


© 2006 Wiley Periodicals, Inc.

A CONTINUOUSLY STEERABLE ARRAY ANTENNA USING MOVABLE DIELECTRIC SLABS ON A COPLANAR WAVEGUIDE

Junho Cha,1 Yasuo Kuga,1 and Sangil Lee2
1 Department of Electrical Engineering, University of Washington, Box 352500, Seattle, WA 98195
2 Electronics Engineering Department, Mokpo National University, Chonman, Korea

Received 20 June 2006

ABSTRACT: A simple steerable array antenna is designed using a movable dielectric phase shifter. The change of the effective dielectric constant at different dielectric slab positions on a coplanar waveguide is used as the phase shifter. The impedance matching and desired phase shift conditions are satisfied at two slab heights, and reflection is designed to be minimized at all slab positions. A four-element steerable array antenna at 5.8 GHz is fabricated and measured for testing purposes. © 2006 Wiley Periodicals, Inc.

Microwave Opt Technol Lett 48: 2222–2227, 2006; Published online in Wiley InterScience (www.interscience.wiley.com). DOI 10.1002/mop.21920

Keywords: steerable array antenna; phase shifter

1. INTRODUCTION

In this paper, we introduce a movable dielectric slab placed close to a coplanar waveguide (CPW) which can be used as a phase shifter for the array antenna. The proposed array antenna consists of a patch array antenna, phase shifter, and feed network with a preset delay line as shown in Figure 1. It is noted that the most significant and difficult part of the simulation and fabrication process is the design of the phase shifter [1]. In order to obtain the optimum combinations of a transmission line (TL) structure and material, several TL structures have been investigated. These include a microstrip TL, a coplanar TL without gaps, and a coplanar TL with gaps. Our study shows that the microstrip TL and coplanar TL without gaps are insensitive to the position of a dielectric slab and are eliminated from consideration. In addition, it is found that a high-$\varepsilon_r$ material such as BaTiO$_3$ is not suited for a phase shifter. It appears that the electromagnetic field perturbation caused by a high-$\varepsilon_r$ material is significant, and the proposed design does not work as a phase shifter. The effective dielectric constant and the characteristic impedance are calculated as a function of slab...
because we are designing a low-cost antenna, we use a CPW structure fabricated on an FR-4 type substrate (IS620 from Iola) which has a thickness of 1.6 mm and $\varepsilon_{\text{sub}} = 3.73$. The CPW has a signal trace width of 2 mm and a ground trace width of 6 mm. The gap between the ground and the signal is 1 mm. Without the dielectric slab ($d = 5$ mm or effectively $d = \infty$), the CPW has a characteristic impedance of $Z_0 = 103 \, \Omega$ and an effective dielectric constant of $\varepsilon_{\text{effective}} = 1.4$. To simplify the fabrication process, we also used dielectric slabs without protruding notches in the initial design. Therefore, when $d = 0$, the CPW gap is filled with air rather than with the dielectric material. The dielectric constant of the slab must be much higher than that of the substrate, but it cannot be too high. It is found that a high-$\varepsilon_r$ material such as BaTiO$_3$ creates a strong electromagnetic field perturbation and is not useful as a slab in our design. We chose the Teflon–ceramic composite with $\varepsilon_r = 10.5$ as a slab. Using HFSS simulations, the desired effective dielectric constant is found to be about $\varepsilon_{\text{effective}} = 7.76$ when $d = 0$. This will determine the length of the $\lambda/2$ section to be 9.32 mm, and the amount of phase shift with respect to the $d = \infty$ condition is 105°. Therefore, if we want to introduce a 105° phase difference among four antenna elements, the length should be 0, $\lambda/2$, $\lambda$, and $3\lambda/2$. Since we cannot find an analytical formula to estimate $\varepsilon_{\text{effective}}$ for $d > 0$, extensive HFSS simulations are conducted for $0 < d < 5$ mm. Because the slab length is set close to the integer multiple of $\lambda/2$ when $d = 0$, the reflection from this slab will be small at $d = 0$. By setting, we can approximate $T$ in Eq. (1) as $T = e^{-j\theta}$. Then the phase change at the slab height $d$ with respect to that without a dielectric slab ($d = \infty$) can approximately be expressed as

$$\theta_d \approx k_0 L_d \left(\varepsilon_{\text{eff}, d} - \varepsilon_{\text{eff}, d = \infty}\right),$$

(2)

where $k_0$ is the wavenumber in free space and $L_d$ is the slab length. $\varepsilon_{\text{eff}, d} = \infty$ represents the effective dielectric constant when the dielectric material is far enough away from the substrate, and $\varepsilon_{\text{eff}, d = \infty}$ represents the effective dielectric constant when the slab height is $d$. The effective dielectric constant for $0 < d < 5$ mm is estimated from this phase. Table 1 presents numerical results for the G-S-G CPW with the center gap for cases with and without the dielectric material. The characteristic impedance and the effective dielectric constant change depending on the distance of the dielectric material from the substrate. As expected, the impedance is matched at $d = 5$ and 0. When $d = 1.25$ mm, there is a slight impedance mismatch, although $S_{11}$ is still close to 1. Figure 2 shows the effective dielectric constant as a function of distance $d$. Beyond $d > 2$ mm, the slab is completely out of the CPW and there is no change in $\varepsilon_{\text{effective}}$. The effective dielectric constant gradually changes from $d = 2$ mm to $d = 0.25$ mm and then increases rapidly at $d = 0$. We chose the phase difference of $-105^\circ$ to $+105^\circ$ between adjacent elements, because the phase difference between $d = 5$ mm and $d = 0$ is $105^\circ$ in Table 1.

**Table 1** Simulated Results at $d = 5$ mm, $d = 1.25$ mm, and $d = 0$

<table>
<thead>
<tr>
<th>Parameter</th>
<th>5</th>
<th>1.25</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_{11}$</td>
<td>0.99</td>
<td>0.91</td>
<td>0.98</td>
</tr>
<tr>
<td>Characteristic impedance ((\Omega))</td>
<td>103</td>
<td>83</td>
<td>51</td>
</tr>
<tr>
<td>Effective dielectric constant</td>
<td>1.4</td>
<td>3.73</td>
<td>7.76</td>
</tr>
<tr>
<td>Phase difference based on $d = 5$ mm</td>
<td>0°</td>
<td>49.5°</td>
<td>105°</td>
</tr>
</tbody>
</table>

2. CONTINUOUS PHASE SHIFTER BASED ON A MOVABLE DIELECTRIC SLAB

The basic concept of the phase shifter is illustrated in Figure 1. The CPW has air gaps between the center signal line and ground lines. As the movable dielectric slab moves closer or into the gap of the CPW, the effective dielectric constant changes and it is given as a function of distance $d$ for a given structure. In this paper, we assume that the slab can be moved continuously from the flash on the substrate ($d = 0$ or very small) to far away from the substrate ($d = \infty$ or $d > 2$ mm in our case).

The width of the signal trace is $S$ and the width of the ground trace is $G_N$. The gap between the ground and the signal is $G$. Substrate thickness is $h$ and the height of the dielectric material is 5 mm. The length of the dielectric material is $l$.

This structure can be modeled as an unmatched TL section (or a layered structure). The transmission coefficient $T$ of a layered structure is given as [2]

$$T = \frac{(1 - \Gamma_1^2) e^{-j\theta}}{1 - \Gamma_1^2 e^{-j\theta}},$$

(1)

where $\Gamma_1$ is the reflection coefficient at the boundary due to a semiinfinite layer and $\theta$ is the phase shift due to a slab. When $\theta$ becomes an integer multiple of $1/2$, it is well known that the reflection from the slab diminishes (or $T$ becomes 1). This is the impedance matching condition. In addition, the phase shift of the slab section when $d$ is changed from $d = \infty$ to $d = 0$ will be related to the effective dielectric constant of these two states [3]. Our primary concern will be a good impedance matching at all values of $d$. First, we set the matched impedance condition at $d = 0$ and $d = \infty$. Since the integer multiple of the $\lambda/2$ condition must be satisfied at $d = 0$, this will determine the available length of each slab. At $d = \infty$ or without slab, the impedance is always matched. The main task, therefore, is to estimate the effective dielectric constant of CPW with a slab on it. This process requires knowledge of the material characteristics, TL structure, and a good 3-D simulation tool. Because we are designing a low-cost antenna, we compare the simulated radiation patterns and the measured radiation patterns of the steerable array antenna at 5.8 GHz.
Figure 2  Effective dielectric constant vs. height d from the substrate. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com]

Figure 3  Simulated S21 and S11 results from d = 0 to d = 5 mm. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com]

3. DESIGN OF THE FEED NETWORK USING THE PRESET DELAY LINES

In order to reduce the number of phase shifters to N-1 where N is the number of arrays, the preset delay line is added to each feed line as shown in Figure 1. The basic concept is illustrated in Figure 4. Suppose the antenna is designed with a phase difference of $-105^\circ$ to $+105^\circ$ between adjacent elements, then the required phases at different antenna elements are shown in Figure 4. The Antenna Element 1 which is shown as S1 in Figure 4. The largest phase shift of 630° is required for Element 4 (S5 in Fig. 4). Therefore, by introducing the preset delay line, we can eliminate one phase shifter.

The CPW has the characteristic impedance of $Z_0 = 103 \Omega$ with $d = 5$ mm and an input impedance of the patch antenna of 103 $\Omega$.

Figure 4  Phase difference among four elements from $-105^\circ$ to $+105^\circ$

The main problem with the proposed phase shifter is that the characteristic impedance also changes when the dielectric slab position is changed from $d = 5$ mm ($Z_0 = 103 \Omega$) to $d = 0$ ($Z_0 = 51 \Omega$). The lowest $Z_0$ occurs at $d = 0$, and thus the circuit must be designed to minimize the reflection at $d = 0$. In order to reduce the unwanted reflection, the effective length of the CPW is set with $d = 0$ to be $m\lambda/2$ where m is an integer. Because a A/2 section does not create a reflection, this will guarantee the impedance matching at $d = 0$. At other slab positions, we estimate the characteristic impedance using HFSS. Table 2 shows the required slab height and the characteristic impedance $Z_0$ for the 4-element array antenna with the phase difference at $-105^\circ$, 0°, and $+105^\circ$. Although the reflection is minimized at $d = 0$ and $d = 5$ mm, we have an impedance mismatch at $d = 0.5$ mm as shown in Table 2. For the element phase differences of $-105^\circ$ to $+105^\circ$, we can obtain the antenna beam scan angle of $-40^\circ$ to $+40^\circ$.

Table 2  Phase Relationship of 4-Element Array at 3 Phase (Slab) Positions: $-105^\circ$, 0, and $+105^\circ$

<table>
<thead>
<tr>
<th>Phase</th>
<th>Distance (mm)</th>
<th>$S_{21}$</th>
<th>$S_{31}$</th>
<th>$S_{41}$</th>
<th>$S_{51}$</th>
<th>$Z_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$-105^\circ$</td>
<td>d=0</td>
<td>0°</td>
<td>210°</td>
<td>420°</td>
<td>630°</td>
<td>51</td>
</tr>
<tr>
<td>0°</td>
<td>d=0.5</td>
<td>0°</td>
<td>105°</td>
<td>210°</td>
<td>315°</td>
<td>77</td>
</tr>
<tr>
<td>$+105^\circ$</td>
<td>d=5</td>
<td>0°</td>
<td>0°</td>
<td>0°</td>
<td>0°</td>
<td>103</td>
</tr>
</tbody>
</table>
The preset delay lines in Figure 6 have $-315^\circ$ for Element 1, $-210^\circ$ for Element 2, and $-105^\circ$ for Element 3, whereas the dielectric slabs introduce a maximum phase shift of $-210^\circ$ for Element 2, $-420^\circ$ for Element 3, and $-630^\circ$ for Element 4. This corresponds to the phase diagram shown in Figure 4. The lengths of the dielectric slabs on the CPW are 20.9, 41.8, and 62.7 mm.

Figure 6 shows the simulated H-plane radiation patterns of a $4 \times 1$ array antenna at 5.8 GHz. Figure 6(a) is for $d = 0$ with the peak at 30°, (b) is for $d = 0.1$ mm with the peak close to 0°, and (c) is for $d = 5$ mm with the peak at $-40^\circ$. Figure 7 shows the measured H-plane radiation pattern of a $4 \times 1$ array antenna for the same three values of $d$. We obtain good agreement for the $d = 0$ and $d = 0.1$ mm cases, but when the slab is on the CPW, the peak of the beam is only at 13°. This discrepancy seems to be due to a small residual gap ($<10$ $\mu$m) between the dielectric slab and conductors, and it is difficult to avoid when using the flat bottom slabs. In order to solve this problem, we added protruding notches.

Figure 5 Photographs of a $4 \times 1$ and $4 \times 2$ array antenna with and without dielectric slabs. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com]

Figure 6 Simulated H-plane radiation patterns of a $4 \times 1$ array antenna at 5.8 GHz. (a) $d = 0$ mm, (b) $d = 0.1$ mm, and (c) $d = 5$ mm. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com]

Figure 7 Measured H-plane radiation patterns of a $4 \times 1$ array antenna at 5.8 GHz. (a) $d = 0$, (b) $d = 0.1$ mm, and (c) $d = 5$ mm. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com]
Figure 8  Phase shifter. A 3-D schematic of a ground-signal-ground (G-S-G) CPW with a movable dielectric slab. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com]

Figure 9  Measured H-plane radiation patterns of a $4 \times 2$ array antenna at 5.8 GHz. (a) $d = 0$ mm with small notches, (b) $d = 0.1$ mm, and (c) $d = 5$ mm. [Color figure can be viewed in the online issue, which is available at www.interscience.wiley.com]
to the flat bottom dielectric slabs, and tested them with a $4 \times 2$ array antenna. This modification makes the shape of slabs similar to the one shown in Figure 8. Figure 9 shows the H-plane radiation patterns of three cases. With the addition of small notches, the antenna beam can now be scanned up to $+40^\circ$.

5. CONCLUSIONS

A novel design of a steerable array antenna has been demonstrated. The phase shifter is based on a movable dielectric slab placed close to a CPW with air gaps. The impedance mismatch can be avoided by choosing the slab dielectric constant and length for the two extreme positions, namely at $d = 0$ and $d = 2 \text{mm}$. It may be possible to further reduce $S_11$ by optimizing the impedance mismatching position at $d > 0$ instead of $d = 0$. We also show that the use of preset delay lines can reduce the number of phase shifters. Although the test antenna is designed for 5.8 GHz, the technique can be applied at a much higher frequency. One possible application is for the 77 GHz automobile collision avoidance radar [6].

ACKNOWLEDGMENTS

This project was supported by National Science Foundation ECS-0424414. The authors thank J. Kajiya and J. Ritcey for useful discussions and suggestions.

REFERENCES


© 2006 Wiley Periodicals, Inc.